Polynomial and Rational Inequalities

UNinverity of Minnesota

## Preliminaries

- Graphing Polynomials
- Graphing Rational Functions
- Interval Notation

Objectives

- Solve Polynomial Inequalities
- Solve Rational Inequalities


## Example 3

$(x+4)(x-3) \geq 0$


The set of all values $x$ for which $(x+4)(x-3) \geq 0$ is

$$
(-\infty,-4] \cup[3, \infty)
$$

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## Poymomia and Raional Inequalites

## Example 1

$f(x)=\frac{(x+3)^{3}(x-2)^{2}}{(x+1)(x-1)^{2}} \geq 0$


The set of all values $x$ for which $\frac{(x+3)^{3}(x-2)^{2}}{(x+1)(x-1)^{2}} \geq 0$ is

$$
(-\infty,-3] \cup(-1,1) \cup(1, \infty)
$$

- Set one side of the inequality equal to zero
- Factor
- Divide the number line by placing the $x$-intercepts and asymptotes
- Analyze the factors to determine on which intervals the function is positive/negative
- For $\leq$ and $\geq$, include the $x$-intercepts as the endpoints of the intervals
- Never include the $x$-values associated with asymptotes, as the function is undefined at these points.

$$
f(x)=\frac{(x+3)^{3}(x-2)^{2}}{(x+1)(x-1)^{2}}
$$



$$
\begin{gathered}
x^{2}<x+6 \\
x^{2}-x-6<0 \\
(x+2)(x-3)<0
\end{gathered}
$$



The set of all values $x$ for which $x^{2}-x-6<0$ is
$(-2,3)$

