	Preliminaries and Objectives	Example 1
Polynomial and Rational Inequalities	Preliminaries • Graphing Polynomials • Graphing Rational Functions • Interval Notation	$f(x) = \frac{(x+3)^3(x-2)^2}{(x+1)(x-1)^2}$
K University of Minnesota	Objectives <ul> <li>Solve Polynomial Inequalities</li> <li>Solve Rational Inequalities</li> </ul>	$\xrightarrow{-+}_{-+} \xrightarrow{++}_{-+} \xrightarrow{++}_{++} \xrightarrow{++}_{++} \xrightarrow{++}_{++} \xrightarrow{++}_{++} \xrightarrow{++}_{++} \xrightarrow{++}_{+-3} \xrightarrow{-1}_{-1} \xrightarrow{+}_{-1} \xrightarrow{+}_{+} \xrightarrow{+} +$
University of Minnesota Polynomial and Rational Inequalities Example 2	University of Minnesota Polynomial and Rational Inequalities Example 3	University of Minnesota Polynomial and Rational Inequalities Example 4
$(x+4)(x-3) \geq 0$	$(x+4)^3(x-3)^2 \le 0$	$x^2 < x + 6$ x <sup>2</sup> - x - 6 < 0 (x + 2)(x - 3) < 0
$(-)(-) (+)(-) (+)(+)$ $+ -4 - 3 + 3$ The set of all values x for which $(x + 4)(x - 3) \ge 0$ is $(-\infty -4) + (3 \infty)$	$(-)(+) \qquad (+)(+) \qquad (+)(+)$ $(-)(+) \qquad (+)(+) \qquad (+)(+)(+) \qquad (+)(+)(+) \qquad (+)(+)(+) \qquad (+)(+)(+) \qquad (+)(+)(+) \qquad (+)(+)(+)(+) \qquad (+)(+)(+)(+)(+)(+) \qquad (+)(+)(+)(+)(+)(+)(+)(+)(+)(+)(+)(+)(+)($	(-)(-) (+)(-) (+)(+) $(+)(+)$ $(+)(-) (+)(+)$ $(+)(+)$ $(+)(-) (+)(+)$ $(+)(+)(+)(+)(+)(+)(+)(+)(+)(+)(+)(+)(+)($
$(-\infty, -4] \cup [0, \infty)$	(-∞, -4] ∪ {0}	(-2,3)

Example 1

$$f(x) = \frac{(x+3)^3(x-2)^2}{(x+1)(x-1)^2} \ge 0$$

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$$\xrightarrow{-+}_{-+} \xrightarrow{++}_{-+} \xrightarrow{++}_{++} \xrightarrow{++}_{++} \xrightarrow{++}_{++} \xrightarrow{++}_{++}$$

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The set of all values x for which  $\frac{(x+3)^3(x-2)^2}{(x+1)(x-1)^2} \ge 0$  is  $(-\infty, -3] \cup (-1, 1) \cup (1, \infty)$ 

## Recap

- Set one side of the inequality equal to zero
- Factor
- Divide the number line by placing the *x*-intercepts and asymptotes

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- Analyze the factors to determine on which intervals the function is positive/negative
- For  $\leq$  and  $\geq$ , include the *x*-intercepts as the endpoints of the intervals
- Never include the *x*-values associated with asymptotes, as the function is undefined at these points.

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