Preliminaries and Objectives

Functions and Notation

The Composition of Functions



University of Minnesota The Composition of Function

g(x) = x - 3

Preliminaries

- Functions
- Function Notation

Objectives

• Define the composition of functions

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$f(x) = x^2$

$$f(t)=t^2$$

$$f(-3) = 9$$

$$f(g(x)) = \left[g(x)\right]^2$$

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The Composition of Function

Composition of Functions

 $f(x) = x^2$

$$f(\bullet) = \bullet$$

$$f(g(x)) = (x-3)$$

Composition of Functions

$$f(x) = \frac{x^2}{}$$
 $g(\bullet) = \bullet - 3$

$$f(g(x)) = (x-3)^2$$

$$g(f(x)) = x^2 - 3$$

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Example 2

$$f(x) = \sqrt{x} \qquad \qquad g(x) = 3x$$

Find f(g(x)) and g(f(x))

$$f(g(x)) = \sqrt{3x}$$

$$g(f(x))=3\sqrt{x}$$

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Recap

Example 3

$$f(x) = \sqrt{x}$$

$$g(x) = x - 6$$

$$h(x) = 3x$$

Find f(g(h(x)))

$$h(x) = 3x$$

$$g(h(x)) = g(3x) = 3x - 6$$

$$f(g(h(x))) = f(3x - 6)$$

$$= \sqrt{3x-6}$$

To find f(g(x)), use the output of g(x) as the input to f(x).