The Composition of Functions
7. Universtry of Minnesota

## Preliminaries

- Functions
- Function Notation

Objectives

- Define the composition of functions

$$
\begin{gathered}
f(x)=x^{2} \\
f(t)=t^{2} \\
f(-3)=9 \\
f(g(x))=[g(x)]^{2}
\end{gathered}
$$

 The Composilion of Functions

## Example 2

$$
f(x)=x^{2} \quad g(\bullet)=\bullet-3
$$

$$
f(g(x))=(x-3)^{2}
$$

$$
g(f(x))=x^{2}-3
$$

$$
\begin{aligned}
& f(x)=\sqrt{x} \quad g(x)=3 x \\
& \text { Find } f(g(x)) \text { and } g(f(x))
\end{aligned}
$$

$$
f(g(x))=\sqrt{3 x}
$$

$$
g(f(x))=3 \sqrt{x}
$$

$$
h(x)=3 x
$$

To find $f(g(x))$, use the output of $g(x)$ as the input to $f(x)$.
(of $f(g(x)$ ), use the outpur $g(x)$ as the input $f(x)$.
$g(h(x))=g(3 x)=3 x-6$

Recap

$$
g(x)=x-6
$$

$$
\text { Find } f(g(h(x)))
$$

$$
h(x)=3 x
$$

$$
f(g(h(x)))=f(3 x-6)
$$

$$
=\sqrt{3 x-6}
$$

$=\sqrt{3 x-6}$

$$
f(x)=\sqrt{x}
$$

