

Factoring



Preliminaries and Objectives

Preliminaries:

- Distributive Law

$$a(b + c) = ab + ac$$

- The FOIL method

Objectives:

- Factor expressions into binomials

Distributive Law

$$3x(x + 4)$$

$$3x^2 + 12x$$

FOIL

$$(2x + 3)(3x - 1)$$

$$6x^2 - 2x + 9x - 3$$

$$6x^2 + 7x - 3$$

FOIL

$$(2x + 3)(2x - 3)$$

$$4x^2 - 6x + 6x - 9$$

$$4x^2 - 9$$

Undo Distributive Law

- Technique: Greatest Common Factor (GCF)

$$3x^2 + 12x$$

$$3 \cdot x \cdot x + 2 \cdot 2 \cdot 3 \cdot x$$

$$3x(x + 4)$$

Example 1

$$2x^4 + 8x^3 - 16x^2$$

$$2x^2(x^2 + 4x - 8)$$

Difference of Squares

- Technique: Difference of Squares

$$4x^2 - 9$$

$$(2x + 3)(2x - 3)$$

Example 2

$$16x^4 - 25$$

$$(4x^2 + 5)(4x^2 - 5)$$

Example 2

$16x^3 - 25$
does not factor

Undoing FOIL

$$3x^2 + 11x - 4$$

$$(3x + 4)(x - 1)$$

$$(3x - 4)(x + 1)$$

$$(3x + 2)(x - 2)$$

$$(3x - 2)(x + 2)$$

$$(3x + 1)(x - 4)$$

$$(3x - 1)(x + 4)$$

Undoing FOIL

$$3x^2 + 11x - 4$$

$$3x^2 + x - 4$$

No

$$(3x + 4)(x - 1)$$

$$3x^2 - x - 4$$

No

$$(3x - 4)(x + 1)$$

$$3x^2 - 4x - 4$$

No

$$(3x + 2)(x - 2)$$

$$3x^2 + 4x - 4$$

No

$$(3x - 2)(x + 2)$$

$$3x^2 - 11x - 4$$

No

$$(3x + 1)(x - 4)$$

$$3x^2 + 11x - 4$$

Yes

$$(3x - 1)(x + 4)$$

Undoing FOIL

$$ax^2 + bx + c \rightarrow (\quad + \quad)(\quad + \quad)$$

$$ax^2 - bx + c \rightarrow (\quad - \quad)(\quad - \quad)$$

$$ax^2 + bx - c \rightarrow (\quad + \quad)(\quad - \quad)$$

$$ax^2 - bx - c \rightarrow (\quad + \quad)(\quad - \quad)$$

Undoing FOIL

- Technique: Grouping

$$6x^3 - 15x^2 + 8x - 20$$

Undoing FOIL

- Technique: Grouping

$$x^3 + 2x^2 - 9x - 18$$

Undoing FOIL

- Technique: Grouping

$$x^3 + 2x^2 - 9x - 18$$

$$(x^2 - 9)(x + 2)$$

Undoing FOIL

- Technique: Grouping

$$x^3 + 2x^2 - 9x - 18$$

$$(x^2 - 9)(x + 2)$$

$$(x + 3)(x - 3)(x + 2)$$