

## Combining Trig Functions and Inverse Trig Functions - Part I



### Preliminaries and Objectives

Preliminaries:

- Trig functions
- Inverse Trig Functions

Objectives:

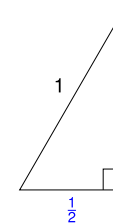
- Find values when trig functions and inverse trig functions are combined.

### Example 1

Find

$$\sin \left( \cos^{-1} \frac{1}{2} \right)$$

↑  
number



### Example 1

Find

$$\sin \left( \cos^{-1} \frac{1}{2} \right)$$

↑  
angle

$\theta = \cos^{-1} \left( \frac{1}{2} \right)$

### Example 1

Find

$$\sin \left( \cos^{-1} \frac{1}{2} \right)$$

↑  
number

$\sin \theta$

### Example 1

Find

$$\sin \left( \cos^{-1} \frac{1}{2} \right) = \sin \left( \frac{\pi}{3} \right) = \frac{\sqrt{3}}{2}$$

### Example 2

Find

$$\sin \left( \cos^{-1} \frac{2}{3} \right)$$

↑  
number

### Example 2

Find

$$\sin \left( \cos^{-1} \frac{2}{3} \right)$$

↑  
angle

$\theta = \cos^{-1} \left( \frac{2}{3} \right)$

### Example 2

Find

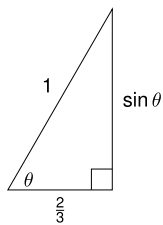
$$\sin \left( \cos^{-1} \frac{2}{3} \right)$$

↑  
number

$\sin \theta$

### Example 2

If  $\cos \theta = \frac{2}{3}$  and  $\theta$  is in quadrant I, find  $\sin \theta$ .



### Example 2

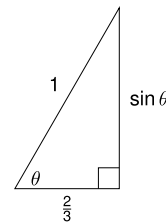
$$\left(\frac{2}{3}\right)^2 + (\sin \theta)^2 = 1$$

$$(\sin \theta)^2 = 1 - \frac{4}{9}$$

$$(\sin \theta)^2 = \frac{5}{9}$$

$$\sin \theta = \frac{\sqrt{5}}{3}$$

$$\sin\left(\cos^{-1}\frac{2}{3}\right) = \frac{\sqrt{5}}{3}$$



### Example 2

$$\sin\left(\cos^{-1}\frac{2}{3}\right)$$

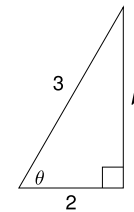
$$b^2 + 2^2 = 3^2$$

$$b^2 = 9 - 4 = 5$$

$$b = \pm\sqrt{5}$$

$$\sin \theta = \frac{b}{3} = \frac{\sqrt{5}}{3}$$

$$\sin\left(\cos^{-1}\frac{2}{3}\right) = \frac{\sqrt{5}}{3}$$

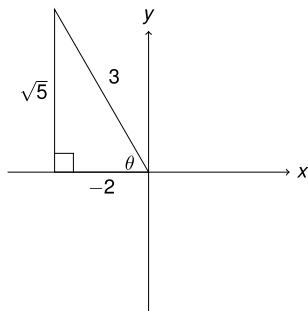


### Example 3 - Negative Values

Find

$$\sin\left(\cos^{-1}\frac{2}{3}\right)$$

$$= \sin \theta = \frac{\sqrt{5}}{3}$$

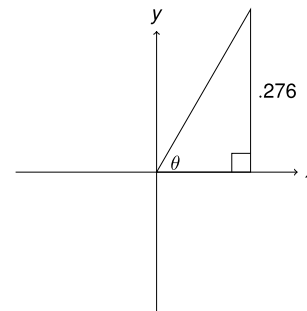


### Example 4

Find

$$\sin\left(\sin^{-1}.276\right)$$

$$\sin \theta = .276$$



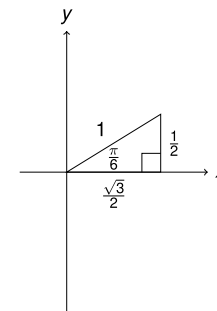
### Example 5

Find

$$\cos^{-1}\left(\sin\frac{\pi}{3}\right)$$

$$= \cos^{-1}\left(\frac{\sqrt{3}}{2}\right)$$

$$= \frac{\pi}{6}$$



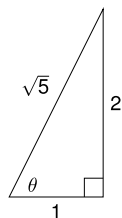
### Example 5

Find  $\cos\left(\tan^{-1}2\right)$

$$\tan \theta = \frac{2}{1}$$

$$\cos \theta = \frac{1}{\sqrt{5}} = \frac{\sqrt{5}}{5}$$

$$\cos\left(\tan^{-1}2\right) = \frac{\sqrt{5}}{5}$$



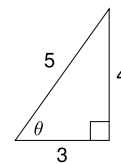
### Example 6

Find  $\tan\left(\cos^{-1}\frac{3}{5}\right)$

$$\theta = \cos^{-1}\left(\frac{3}{5}\right)$$

$$\tan \theta = \frac{4}{3}$$

$$\tan\left(\cos^{-1}\frac{3}{5}\right) = \frac{4}{3}$$



### Example 7

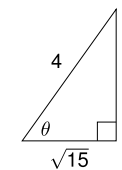
Find  $\sec\left(\sin^{-1}\frac{1}{4}\right)$

$$\theta = \sin^{-1}\frac{1}{4}$$

$$\cos \theta = \frac{\sqrt{15}}{4}$$

$$\sec \theta = \frac{4}{\sqrt{15}} = \frac{4\sqrt{15}}{15}$$

$$\sec\left(\sin^{-1}\frac{1}{4}\right) = \frac{4\sqrt{15}}{15}$$



## Example 8

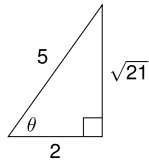
$$\tan\left(\sec^{-1}\frac{5}{2}\right)$$

$$= \tan\left(\cos^{-1}\frac{2}{5}\right)$$

$$\theta = \cos^{-1}\frac{2}{5}$$

$$\tan\theta = \frac{\sqrt{21}}{2}$$

$$\tan\left(\sec^{-1}\frac{5}{2}\right) = \frac{\sqrt{21}}{2}$$



## Recap

- Inputs to inverse trig functions give information about the lengths of sides of a triangle.
- Label a triangle using this information.
- Find the missing side by the Pythagorean Theorem
- Read the values of the other trig functions from the triangle