### **Binomial Probabilities - Part II**



# **Preliminaries and Objectives**

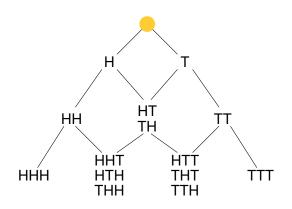
#### **Preliminaries**

- Basic Probability (AND, OR, NOT)
- Pascal's Triangle
- Combinations
- Binomial Probabilities p = 1/2
- Random Variables

#### Objectives

 Calculate probabilities in successive trials with only two outcomes, either succeed or fail.

# Flip three coins



$$P(H=3)=\frac{1}{8},\ P(H=2)=\frac{3}{8},\ P(H=1)=\frac{3}{8},\ P(H=0)=\frac{1}{8}$$

## **Unequally likely outcomes**

A basketball player shoots 70% from the free throw line. Let X = the number of shots made on two attempts.

X =	outcomes	probability
0	00	(.3)(.3) = .09
1	●○ , ○●	(.7)(.3) + (.3)(.7) = .42
2	••	(.7)(.7) = .49

## **Unequally likely outcomes**

A basketball player shoots 70% from the free throw line. Let X = the number of shots made on five attempts. What is the probability that three of the five shots are made?

$$P(\bullet \bullet \bullet \circ \circ) = P(\bullet \bullet \circ \bullet \circ) = \dots (.7)(.7)(.3)(.3) = (.7)(.7)(.3)(.7)(.3) = (.7)^3(.3)^2$$

$$P(X = 3) = {5 \choose 3}(.7)^3(.3)^2 = .3087$$

## **Binomial Probability Formula**

Let p = probability of success on a single trial.

Let q = 1 - p = probability of failure on a single trial.

Let *X* be a random variable that counts the number of successes in *n* independent trials.

### **Binomial Probability**

$$P(X=k) = \binom{n}{k} p^k q^{n-k}$$

where  $\binom{n}{k}$  is the  $k^{th}$  entry in row n of Pascal's Triangle.

### **Exercise**

Find the probability that a 65% free throw shooter will make 3 of 4 attempts.

#### Solution:

$$P(X=3) = {4 \choose 3}(.65)^3(.35) = 4(.65)^3(.35) = .384475$$