# Binomial Probabilities - Part II 

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## Preliminaries and Objectives

Preliminaries

- Basic Probability (AND, OR, NOT)
- Pascal's Triangle
- Combinations
- Binomial Probabilities $p=1 / 2$
- Random Variables

Objectives

- Calculate probabilities in successive trials with only two outcomes, either succeed or fail.


## Flip three coins



## Unequally likely outcomes

A basketball player shoots $70 \%$ from the free throw line. Let $X=$ the number of shots made on two attempts.

| $X=$ | outcomes | probability |
| :---: | :---: | ---: |
| 0 | $\circ \circ$ | $(.3)(.3)=.09$ |
| 1 | $\bullet \circ, \circ$ | $(.7)(.3)+(.3)(.7)=.42$ |
| 2 | $\bullet$ | $(.7)(.7)=.49$ |

## Unequally likely outcomes

A basketball player shoots $70 \%$ from the free throw line. Let $X=$ the number of shots made on five attempts. What is the probability that three of the five shots are made?





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$P(\bullet \bullet \bullet \circ) \quad=P(\bullet \bullet \bullet \circ) \quad=\ldots$
$(.7)(.7)(.7)(.3)(.3)=(.7)(.7)(.3)(.7)(.3)=(.7)^{3}(.3)^{2}$
$P(X=3)=\binom{5}{3}(.7)^{3}(.3)^{2}=.3087$

## Binomial Probability Formula

Let $p=$ probability of success on a single trial.
Let $q=1-p=$ probability of failure on a single trial.
Let $X$ be a random variable that counts the number of successes in $n$ independent trials.

## Binomial Probability

$$
P(X=k)=\binom{n}{k} p^{k} q^{n-k}
$$

where $\binom{n}{k}$ is the $k^{\text {th }}$ entry in row $n$ of Pascal's Triangle.

## Exercise

Find the probability that a $65 \%$ free throw shooter will make 3 of 4 attempts.

## Solution:

$$
P(X=3)=\binom{4}{3}(.65)^{3}(.35)=4(.65)^{3}(.35)=.384475
$$

